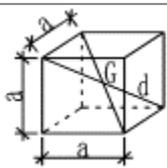
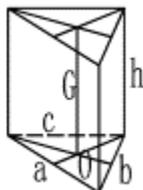
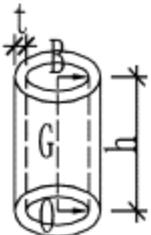
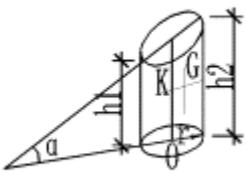
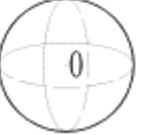
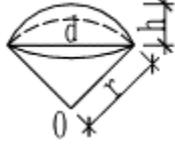
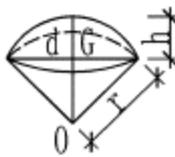
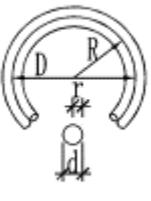
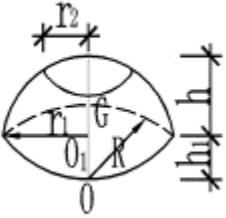
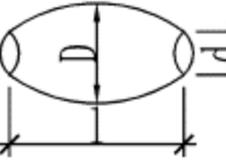
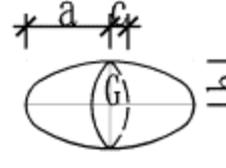
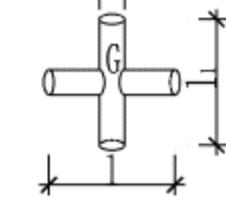
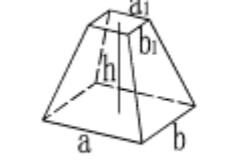
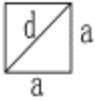
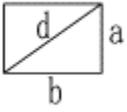
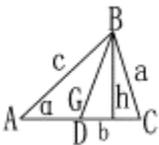
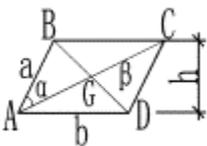
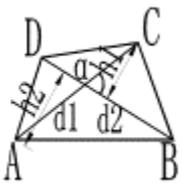
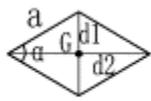
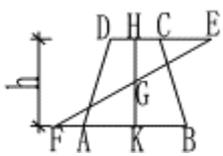


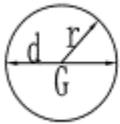
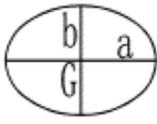
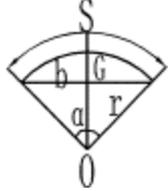
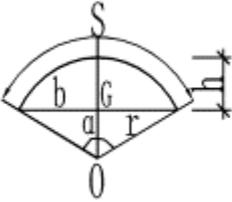
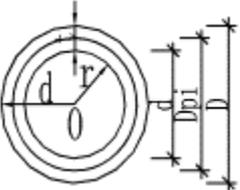
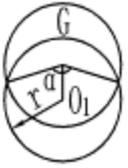
## 多面体的体积和表面积

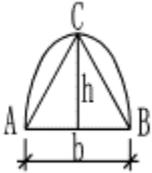
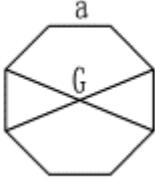
	图形	尺寸符号	体积( $V$ )底面积( $F$ ) 表面积( $S$ )侧面积( $S_1$ )
立方体		$a$ -棱 $d$ -对角线 $S$ -表面积 $S_1$ -侧表面积	$V = a^3$ $S = 6a^2$ $S_1 = 4a^2$
长方体 ∧ 棱柱 ∨		$a, b, h$ -边长 $O$ -底面对角线的交点	$V = a \cdot b \cdot h$ $S = 2(a \cdot b + a \cdot h + b \cdot h)$ $S_1 = 2h(a + b)$ $d = \sqrt{a^2 + b^2 + h^2}$
三棱柱		$a, b, h$ -边长 $h$ -高 $F$ -底面积 $O$ -底面中线的交点	$V = F \cdot h$ $S = (a + b + c) \cdot h + 2F$ $S_1 = (a + b + c) \cdot h$
棱锥		$f$ -一个组合三角形的面积 $n$ -组合三角形的个数 $O$ -锥底各对角线交点	$V = \frac{1}{3} F \cdot h$ $S = n \cdot f + F$ $S_1 = n \cdot f$
棱台		$F_1, F_2$ -两平行底面的面积 $h$ -底面间距离 $a$ -一个组合梯形的面积 $n$ -组合梯形数	$V = \frac{1}{3} h(F_1 + F_2 + \sqrt{F_1 F_2})$ $S = an + F_1 + F_2$ $S_1 = an$
圆柱和空心圆柱 ∧ 管 ∨		$R$ -外半径 $r$ -内半径 $t$ -柱壁厚度 $p$ -平均半径 $S_1$ -内外侧面积	圆柱: $V = \pi R^2 \cdot h$ $S = 2\pi R \cdot h + 2\pi R^2$ $S_1 = 2\pi R \cdot h$ 空心直圆柱: $V = \pi h(R^2 - r^2) = 2\pi p t h$ $S = 2\pi(R + r)h + 2\pi(R^2 - r^2)$ $S_1 = 2\pi h(R + r)$

斜线直圆柱		$h_1$ - 最小高度 $h_2$ - 最大高度 $r$ - 底面半径	$V = \pi r^2 \cdot \frac{h_1 + h_2}{2}$ $S = \pi r (h_1 + h_2) + \pi r^2 \cdot \left(1 + \frac{1}{\cos \alpha}\right)$ $S_1 = \pi r (h_1 + h_2)$
直圆锥		$r$ - 底面半径 $h$ - 高 $l$ - 母线长	$V = \frac{1}{3} \pi r^2 h$ $S_1 = \pi r \sqrt{r^2 + h^2} = \pi r l$ $l = \sqrt{r^2 + h^2}$ $S = S_1 + \pi r^2$
圆台		$R, r$ - 底面半径 $h$ - 高 $l$ - 母线	$V = \frac{\pi h}{3} \cdot (R^2 + r^2 + Rr)$ $S_1 = \pi l (R + r)$ $l = \sqrt{(R - r)^2 + h^2}$ $S = S_1 + \pi (R^2 + r^2)$
球		$r$ - 半径 $d$ - 直径	$V = \frac{4}{3} \pi r^3 = \frac{\pi d^3}{6} = 0.5236 d^3$ $S = 4 \pi r^2 = \pi d^2$
球扇形 球楔		$r$ - 球半径 $d$ - 弓形底圆直径 $h$ - 弓形高	$V = \frac{2}{3} \pi r^2 h = 2.0944 r^2 h$ $S = \frac{\pi r}{2} (4h + d) = 1.57 r (4h + d)$
球缺		$h$ - 球缺的高 $r$ - 球缺半径 $d$ - 平切圆直径 $S_{\text{曲}}$ - 曲面面积 $S$ - 球缺表面积	$V = \pi h^2 \left(r - \frac{h}{3}\right)$ $S_{\text{曲}} = 2 \pi r h = \pi \left(\frac{d^2}{4} + h^2\right)$ $S = \pi h (4r - h)$ $d^2 = 4h(2r - h)$
圆环体 胎		$R$ - 圆球体平均半径 $D$ - 圆环体平均半径 $d$ - 圆环体截面直径 $r$ - 圆环体截面半径	$V = 2 \pi r^2 R \cdot r^2 = \frac{1}{4} \pi^2 D d^2$ $S = 4 \pi r^2 R r = \pi^2 D d = 39.478 R r$

球带体		<p><math>R</math> - 球半径  <math>r_1, r_2</math> - 底面半径  <math>h</math> - 腰高  <math>h_1</math> - 球心<math>O</math>至带底圆心<math>O_1</math>的距离</p>	$V = \frac{\pi h}{8} (3R_1^2 + 3R_2^2 + h^2)$ $S_1 = 2\pi R h$ $S = 2\pi R h + \pi(r_1^2 + r_2^2)$
桶形		<p><math>D</math> - 中间断面直径  <math>d</math> - 底直径  <math>l</math> - 桶高</p>	<p>对于抛物线形桶体</p> $V = \frac{\pi l}{15} (2D^2 + Dd + \frac{3}{4}d^2)$ <p>对于圆形桶体</p> $V = \frac{\pi d^2}{12} (2D^2 + d^2)$
椭球体		<p><math>a, b, c</math> - 半轴</p>	$v = \frac{4}{3} abc\pi$ $S = 2\sqrt{2} \cdot b \cdot \sqrt{a^2 + b^2}$
交叉圆柱体		<p><math>r</math> - 圆柱半径  <math>l, l_1</math> - 圆柱长</p>	$V = \pi r^2 (l + l_1 - \frac{2r}{3})$
梯形体		<p><math>a, b</math> - 下底边长  <math>a_1, b_1</math> - 上底边长  <math>h</math> - 上、下底边距离 (高)</p>	$V = \frac{h}{6} [(2a + a_1)b + (2a_1 + a)b_1]$ $= \frac{h}{6} [ab + (a + a_1)(b + b_1) + a_1b_1]$
常用图形求面积公式			
图形	尺寸符号	面积 (F) 表面积 (S)	

正方形		$a$ - 边长 $d$ - 对角线	$F = a^2$ $a = \sqrt{F} = 0.77d$ $d = 1.414a = 1.414\sqrt{F}$
长方形		$a$ - 短边 $b$ - 长边 $d$ - 对角线	$F = a \cdot b$ $d = \sqrt{a^2 + b^2}$
三角形		$h$ - 高 $l = \frac{1}{2}$ 周长 $a, b, c$ - 对应角 A, B, C 的边长	$F = \frac{bh}{2} = \frac{1}{2}ab\sin C$ $l = \frac{a+b+c}{2}$
平行四边形		$a, b$ - 棱边 $h$ - 对边间的距离	$F = b \cdot h = a \cdot b \sin \alpha$ $= \frac{AC \cdot BD}{2} \sin \beta$
任意四边形		$d_1, d_2$ - 对角线 $\alpha$ - 对角线夹角	$F = \frac{d_2}{2}(h_1 + h_2)$ $= \frac{d_1 d_2}{2} \sin \alpha$
正多边形		$r$ - 内切圆半径 $R$ - 外接圆半径 $a = 2\sqrt{R^2 - r^2}$ - 一边 $a - 180^\circ : n$ ( $n$ - 边数) $p$ - 周长 = $an$	$F = \frac{n}{2} R^2 \sin 2\alpha$ $= \frac{pr}{2}$
菱形		$d_1, d_2$ - 对角线 $a$ - 边 $\alpha$ - 角	$F = a^2 \sin \alpha = \frac{d_1 d_2}{2}$
梯形		$CE = AF$ $AF = CD$ $a = CD$ (上底边) $b = AB$ (下底边) $h$ - 高	$F = \frac{a+b}{2} \cdot h$

圆形		$r$ - 半径 $d$ - 直径 $p$ - 圆周长	$F = \pi r^2 = \frac{1}{4} \pi d^2$ $= 0.785 d^2 = 0.07958 p^2$ $p = \pi d$
椭圆形		a-b-主轴	$F = (\pi/4) a \cdot b$
扇形		$r$ - 半径 $s$ - 弧长 $\alpha$ - 弧s的对应中心角	$F = \frac{1}{2} r \cdot s = \frac{\alpha}{360} \pi r^2$ $s = \frac{\alpha \pi}{180} r$
弓形		$r$ - 半径 $s$ - 弧长 $\alpha$ - 中心角 $b$ - 弦长 $h$ - 高	$F = \frac{1}{2} r^2 \left( \frac{\alpha \pi}{180} - \sin \alpha \right)$ $= \frac{1}{2} [r(s - b) + bh]$ $s = r \cdot \alpha = \frac{\pi}{180} r \cdot \alpha = 0.0175 r \cdot \alpha$ $h = r - \sqrt{r^2 - \frac{1}{4} b^2}$
圆环		$R$ - 外半径 $r$ - 内半径 $D$ - 外直径 $d$ - 内直径 $t$ - 环宽 $D_{pj}$ - 平均直径	$F = \pi(R^2 - r^2)$ $= \frac{\pi}{4}(D^2 - d^2) = \pi \cdot D_{pj} t$
部分圆环		$R$ - 外半径 $r$ - 内半径 $D$ - 外直径 $d$ - 内直径 $t$ - 环宽 $R_{pj}$ - 圆环平均直径	$F = \frac{\alpha \pi}{360} (R^2 - r^2)$ $= \frac{\alpha \pi}{180} R_{pj} \cdot t$
新月形		$L$ - 两个圆心间的距离 $d$ - 直径	$F = r^2 \left( \pi - \frac{\pi}{180} \alpha + \sin \alpha \right) = r^2 \cdot P$ $P = \pi - \frac{\pi}{180} \alpha + \sin \alpha$ $P$ 值见下表

	L d/10	2d/10 3d/10 4d/10	5d/10 6d/10 7d/10
	P 0.40	0.79 1.18 1.56	1.91 2.25 2.55
抛物线形		$b$ - 底边 $h$ - 高 $l$ - 曲线长 $S$ - $\triangle ABC$ 的面积	$l = \sqrt{b^2 + 1.3333h^2}$ $F = \frac{2}{3}b \cdot h = \frac{4}{3} \cdot S$
等多边形		$a$ - 边长 $K_i$ - 系数指多边形的边数	$F = K \cdot a^2$ 三边形 $K_3 = 0.433$ 四边形 $K_4 = 1.000$ 五边形 $K_5 = 1.720$ 六边形 $K_6 = 2.598$ 七边形 $K_7 = 3.614$ 八边形 $K_8 = 4.828$ 九边形 $K_9 = 6.182$ 十边形 $K_{10} = 7.694$